Advanced School in Artificial Intelligence Bertinoro (FC), 17-28 luglio 2023

## Making Decisions with AI

## Roberto Amadini

## Choice vs. Decision

- What is the difference between choice and decision?



## Choice vs. Decision

- What is the difference between choice and decision?
- Interchangeable notions, used often as synonyms
- Choice ~ option, opportunity, "possible branches"
- Decision $\sim$ act of picking one (or more) choice(s) according to some criteria

- In natural language, no difference between "making a choice" or "taking a decision"
- From our perspective, the distinction will be more sharp
- Given a range of (not) possible choices how to make the "right" decisions?
- https://www.moralmachine.net/


## Decision Support Systems

- A Decision Support System (DSS) is a framework supporting the decision-making activities of people/organizations
- DSS focuses on facilitating decision-making rather than fully automating it
- E.g., Clinical Decision Support Systems (CDSS)
- Many ethical, security, transparency, legal issues are involved
- Al and Machine Learning in particular, play a big role here, e.g.
- Predictions of risks
- Artificial vision
- Automated diagnosis


## ChatGPT vs DSS

- ChatGPT is a chatbot launched by OpenAl in November 2022
- Built on top of OpenAl's GPT-3 language model to predict what next word is
- Tuned with both supervised/reinforcement learning (175 billion parameters)
- Based on Transformer-based deep neural networks for NLP
- Following the release of ChatGPT, OpenAI was valued at $\$ 29$ billion
- It can provide impressive performance!
- https://www.theguardian.com/australia-news/2023/ian/10/universities-to-return-to-pen-and-paper-exams-after-students-caught-using-ai-to-write-essays
- It may suffer from hallucination (incorrect/nonsense answers) and algorithmic bias (systematic errors "privileging unfair outcomes")
- Is ChatGPT a DSS?


## ChatGPT vs DSS

Un caso esemplare è quello di un sindaco australiano che secondo il chatbot era stato condannato per corruzione; tutto falso, tanto che ha ottenuto che ChatGpt non risponda a chi chiede informazione su di lui.Insomma, se OpenAI non riesce a rettificare questi errori - e può essere difficile o impossibile, dato il funzionamento dell'algoritmo - almeno deve permettere a chiunque di essere esclusi dal sistema.

LA STORIA

## «ChatGpt? Una droga: così l'intelligenza artificiale mi ha rubato la vita»

Il chatbot di OpenAi può creare dipendenza? Il racconto di Daniele Amadio al Corriere della Sera: "Restavo incollato al computer fino alle sei del mattino, ho abbandonato amici e fidanzate. Poi mi sono imposto uno stop..."
"Molla tua moglie e sposami!": Chat Gpt 'impazzisce' e risponde così ad un utente. Gli esperti: "Ha doppia personalità, sembra un adolescente con tendenze maniaco-depressive"

ChatGPT risponde a chi chiede consigli sulla propria salute. E lo fa meglio dei medici. Occhio però: il rischio che dia informazioni sbagliate è dietro l'angolo.

ChatGPT, chi sono i lavoratori sottopagati che lo fanno funzionare

I trainer degli algoritmi sono impiegati da aziende terze e pagati cifre bassissime. Ma
senza di loro i chatbot non potrebbero funzionare

## DSS, AI and Optimisation

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- ...But Al is not just machine learning and robots!
- Starting from the '90s, researchers started to apply Al to optimisation for having more flexible and intelligible techniques w.r.t. traditional mathematical approaches
- Before that, mainly mathematical tools and methods (Operations Research): dynamic programming, (non-)linear programming, ...
- Al-based optimisation can improve the decision support in many areas
- Planning factory assembly
- Resource/task allocation
- Roster scheduling
- Budgeting
- ....


## Why not sub-symbolic?

- Why not using sub-symbolic AI?
- It requires powerful hardware
- It requires a lot of data
- It does not guarantee a sound answer
- It cannot explain an answer
- It is often "black-box": we don't write a model, we prepare data and maybe tune parameters of a certain ML approach


## Why not sub-symbolic?

- Why not using sub-symbolic AI?
- It requires doesn't require powerful hardware
- It requires doesn't' require a lot of data
- It does net guarantee a sound answer - possibly optimal
- It cannet explain an answer (including failures)
- It is often "black-box"-"gray-box": we don't write a model, although we don't see how it is solved


## DSS and Intelligence

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- What makes a DSS for optimisation intelligent?
- What does it mean intelligent? From Wikipedia:
"Intelligence has been defined in many ways: the capacity for logic, understanding, selfawareness, learning, emotional knowledge, reasoning, planning, creativity, critical thinking, and problem-solving [...] "
- We borrow the definition of Intelligent DSS (IDS) from the book Building Decision Support Systems: Using MiniZinc by M. Wallace (2020)


## Building

Decision
Support Systems


## Intelligent DSS

- It defines a DSS intelligent if:
- It can do tasks which would encourage us to call "intelligent" a person capable of doing such tasks
- In this context, intelligence does not refer to systems behaving like humans, have consciousness or are able to think
- It accomplishes tasks complicated enough that the present-day observer cannot see how they are done
- It does things that are currently clever IT
- E.g., in the 70s an electronic calculator was considered a clever gadget, while today is perceived as a very simple tool - probably a useless tool...


## What decisions?

- IDS can help organisations to take better decisions
- The decisions made by and for an organisation have different types and impact
- Strategic decisions
- Long term ( $\geq 5$ years), critical: human expertise needed
- Tactical decisions
- Mid-term (weeks/months), the core application of IDS
- Operational decisions
- Short term (up to few days), no complex IDS needed


## Example: hospitality

- Strategic decisions
- Opening / Moving / Closing a restaurant
- Changing target customers
- Tactical decisions
- Rostering
- Ordering supplies
- Operational decisions

- Replacing last minute sick employee
- Food preparation/serving


## Combination of choices

- An IDS enhances decision-making by enabling the "best" choices according to given goal(s)
- "Acting rationally"
- IDS models and handles combination of choices to take "optimal" decisions
- The overall number of possible combinations can be huge even if the number of individual decisions and choices is limited!



## Combination of choices

- E.g., Sudoku puzzle
- $\leq 81$ decisions to take (the numbers to be filled in each cell)
- $\leq 9$ choices for each decision (each cell is filled with a digit in 1..9)

- The number of feasible combinations for Sudoku is however much greater than $81 \times 9=729$. In fact, it is $6670903752021072936960 \approx 6.671 \times 10^{21}$
- http://www.afjarvis.staff.shef.ac.uk/sudoku/sudoku.pdf
- Even when the no. of decisions and choices is relatively small, the no. of combination of choices can be huge!
- Often, we have constraints restricting the no. of feasible combinations
- Often, we also aim to find the best feasible combination!


## Combination of choices

- How to solve Sudoku with sub-symbolic AI?


## Combination of choices

- How to solve Sudoku with sub-symbolic AI? Let's ask ChatGPT

1. Data preparation: Prepare a dataset of Sudoku puzzles and their solutions for training and evaluation purposes.
2. Model training: Train a sub-symbolic Al model, such as a neural network or a genetic algorithm, to learn a policy or a heuristic that guides the search process. This training can involve techniques like reinforcement learning or evolutionary optimization.
3. Search and inference: Utilize the trained model to guide the search process. Start with an incomplete Sudoku puzzle and use the model to make predictions or generate candidate solutions. Apply search algorithms like backtracking or local search to explore the solution space based on the model's guidance.
4. Evaluation and refinement: Evaluate the generated solutions against the puzzle's constraints and scoring metrics. Refine the model and search algorithms based on the performance feedback to improve the solving accuracy.

## Combination of choices

- How to solve Sudoku with symbolic AI? We shall see it!


Finished in 130msec

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## Fundamentals of Modeling

## Roberto Amadini

## Selecting from a set

- Example: suppose we have a set $\mathbf{S}$ of numbers and consider the following problems:
- Are there $\mathbf{N}$ numbers in $\mathbf{S}$ with a total over a number $\mathbf{K}$ ?
- E.g., if $S=\{7,10,23,13,4,16\}$
- $N=4, K=50 \rightarrow$ ?


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- $N=2, K=50 \rightarrow$ ?


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- Are there $\mathbf{N}$ numbers in $\mathbf{S}$ with a total equal to a number $\mathbf{K}$ ?
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- $\mathrm{N}=3, \mathrm{~K}=50 \rightarrow \mathrm{NO}$ !


## Selecting from a set

- Example: suppose we have a set $\mathbf{S}$ of numbers and consider the following problems:
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- $N=4, K=50 \rightarrow$ YES: $\{13,23,10,4\}$
- $\mathrm{N}=3, \mathrm{~K}=50 \rightarrow \mathrm{NO}$ !
- These are examples of decision problems: the answer is either YES or NO
- Are they "easy" or "hard" to solve?


## Selecting from a set

- Example: suppose we have a set $\mathbf{S}$ of numbers and consider the following problems:
- Are there $\mathbf{N}$ numbers in $\mathbf{S}$ with a total over a number $\mathbf{K}$ ?
- Easy to solve (polynomial time w.r.t. |S|)
- Not very interesting...
- Are there $\mathbf{N}$ numbers in $\mathbf{S}$ with a total equal to a number $\mathbf{K}$ ?
- Hard to solve (exponential time w.r.t. /S/)
- Variant of subset-sum: https://en.wikipedia.org/wiki/Subset_sum_problem
- Solving "efficiently" the subset-sum problem would imply P = NP
- And so, what?


## P vs NP dilemma

- P: class of problems that can be solved in polynomial time (~reasonable time)
- NP: class of all problems which solution can be verified in polynomial time
- E.g., verify that $\{13,23,10,4\}$ has 4 elements and its sum is 50
- A problem in $P$ is always in $N P: P \subseteq N P$
- If we can find the solution of a problem in "reasonable" time, verifying its soundness cannot be slower...
- But what if NP $\subseteq$ P ? Given a generic NP problem, which solution is verifiable in "reasonable" time, does it exist an algorithm solving it in "reasonable" time?
- If so, P = NP (otherwise, $\mathrm{P} \neq \mathrm{NP}$ )


## P vs NP dilemma

- The P-NP dilemma is a major open problem in Computer Science
- \$1.000.000 prize for solving it
- Finding that $\mathrm{P}=\mathrm{NP}$ could be revolutionary
- Cryptosystems break down
- HTTPS no more secure
- Optimization becomes "easy"
- And ML as well
- The whole world could change!



## P vs NP dilemma

- If a problem is "at least as hard as any other problem in NP" is called NP-hard
- If it is also in NP, it is called NP-complete
- Why do we care? Because several problems faced by IDS are (NP-)hard!
- Optimizing tasks/resource allocation, scheduling, planning, ...
- A salesperson claiming that his DSS can optimally solve medium to large industrial problems (packing, delivering, scheduling, ...) is either a charlatan or he doesn't know what he's selling!
- We can be lucky on some particular instances
- But at present no one could find a way to efficiently solve them in general
- The subset-sum problem seen above is NP-hard in general


## P vs NP vs ChatGPT

As an AI language model, I can help you understand and explain NP-hard problems, but I cannot guarantee an efficient solution for all instances of NP-hard problems. NP-hard problems are a class of computational problems that are believed to require a significant amount of computational resources to solve optimally.

NP-hard stands for "nondeterministic polynomial-time hard." These problems are characterized by the property that if there exists an efficient algorithm to solve one of them, then there exists an efficient algorithm for solving all problems in the complexity class NP (nondeterministic polynomial-time). However, no efficient algorithm has been discovered yet for solving all instances of NP-hard problems.

Some well-known NP-hard problems include the traveling salesman problem, the knapsack problem, and the Boolean satisfiability problem. These problems have practical applications in various fields, such as logistics, optimization, and cryptography.

## P vs NP vs ChatGPT

Can deep learning solve NP-hard problems?Deep learning, as a subfield of machine learning, is primarily used for pattern recognition, feature extraction, and prediction tasks. While deep learning has achieved remarkable success in various domains such as image and speech recognition, it is not inherently designed to solve NP-hard problems efficiently.

NP-hard problems typically involve combinatorial or optimization aspects that require exploring a large search space. Deep learning models, such as neural networks, are not directly suited for solving such problems because they are not explicitly designed to handle discrete decision-making or combinatorial optimization.

However, deep learning can still play a role in solving certain aspects of NP-hard problems. For example, it can be used for feature extraction or representation learning, which can then be fed into other algorithms or optimization techniques specifically designed for NP-hard problems.

Additionally, deep reinforcement learning, a combination of deep learning and reinforcement learning, has shown promise in tackling some combinatorial optimization problems. By using neural networks to approximate value functions or policies, deep reinforcement learning can guide the search or decision-making process in solving certain NP-hard problems.

In summary, while deep learning alone is not typically used as a direct solution method for NP-hard problems, it can be employed in conjunction with other techniques or algorithms to address specific aspects of these challenging problems.

## Knapsack

- Knapsack problem: given a set of items, each with a weight and a value, determine the number of each item to put in a knapsack so that the total weight does not exceed a given limit and the total value is maximal
- Optimization problem: we maximize the total value
- Generalization of subset-sum problem
- Many variants: decision version, 0-1 knapsack, size/volume constraints, ...

- In general knapsack is (NP-)hard
- Some variants are easy, e.g., the fractional knapsack where we can break down items


## Knapsack

- Ok, knapsack and subset-sum are hard to solve, and so what?
- Thinking to the above problems as some theoretical, useless stuff is absolutely wrong!
- The knapsack problem is fundamental for several logistics applications
- loading ships, trucks, planes, space shuttles, ...
- The key is to model a real-life problem into a "toy problem" which is both:
- simple enough to be encoded and solved "efficiently"
- expressive enough to properly approximate the original problem
- possibly similar to other well-studied problems (e.g., knapsack, TSP, ...)


## Travelling Salesman Problem

- Traveling Salesman problem: given $\mathbf{N}$ cities and their distance, what is the minimal-distance tour visiting each city exactly once?
- TSP is a fundamental routing problem, with several variants and applications in planning and logistics
- As the knapsack problem, is (NP-)hard to solve
- But we can model it quite easily
- Different models are possible!



## Modelling and solving

- So, how Al can be used to take optimal decisions?
- The first step is identifying the problem components and their interaction
- What should we decide and what we cannot? Which options do we have? What are the requirements? What is the goal? How to rank different solutions?
- This leads to a model of the problem: how to properly abstract these components?
- What are the (not) relevant features of each component?
- Finally, a "special agent" (a.k.a. the solver) solves the problem for us
- We specify what to solve rather than how to do it



## Modelling and solving



## Modeling

- To model combinatorial problems like subset-sum and knapsack we need to identify:
- Variables: model the possible decisions
- A value assigned to a variable represents a choice made for that decision
- Domains: model the possible choices for a decision
- Often a finite set of choices
- Constraints: define the requirements ruling out incompatible choices
- Domains are a particular case of constraints defining the possible choices for a decision
- Objective [optional]: defines the goal, i.e., what we need to maximize or minimize
- Parameters: the input values specifying an instance of the model


## Example: Sudoku

- E.g., a model for the Sudoku problem
- Variables: model the possible decisions
- A value assigned to a variable represents a choice made
- Domains: model the possible choices for a decision
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| 5 | 3 |  |  | 7 |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6 |  |  | 1 | 9 | 5 |  |  |  |
|  | 9 | 8 |  |  |  |  | 6 |  |
| 8 |  |  |  | 6 |  |  |  | 3 |
| 4 |  |  | 8 |  | 3 |  |  | 1 |
| 7 |  |  |  | 2 |  |  |  | 6 |
|  | 6 |  |  |  |  | 2 | 8 |  |
|  |  |  | 4 | 1 | 9 |  |  | 5 |
|  |  |  |  | 8 |  |  | 7 | 9 |

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- Objective [optional]: something that we need to maximize or minimize
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## Example: Sudoku

- E.g., a model for the Sudoku problem
- Variables: model the possible decisions
- $9 \times 9=\mathbf{8 1}$ variables, one for each cell of the table
- Domains: model the possible choices for a decision
- For each variable, we can pick a value in $1 . .9$ only

| 5 | 3 |  |  | 7 |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6 |  |  | 1 | 9 | 5 |  |  |  |
|  | 9 | 8 |  |  |  |  | 6 |  |
| 8 |  |  |  | 6 |  |  |  | 3 |
| 4 |  |  | 8 |  | 3 |  |  | 1 |
| 7 |  |  |  | 2 |  |  |  | 6 |
|  | 6 |  |  |  |  | 2 | 8 |  |
|  |  |  | 4 | 1 | 9 |  |  | 5 |
|  |  |  |  | 8 |  |  | 7 | 9 |

- Constraints: define the requirements ruling out incompatible choices
- Values on the same row, column, and grid are all different
- Objective [optional]: nothing to minimize/maximize!
- Parameters: the initial values on the grid


## Example: Subset-sum

- E.g., a model for subset-sum problem: are there $\mathbf{N}$ numbers in a set $\mathbf{S}$ adding up to $\mathbf{K}$ ?
- Variables: model the possible decisions
- N variables $\mathrm{X}_{1}, \mathrm{X}_{2}, \ldots, \mathrm{X}_{\mathrm{N}}$ corresponding to the N numbers
- Domains: model the possible choices for a decision
- ?


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- Domains: model the possible choices for a decision
- For each variable, we can pick a value in $S$ only


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- E.g., a model for subset-sum problem: are there $\mathbf{N}$ numbers in a set $\mathbf{S}$ adding up to $\mathbf{K}$ ?
- Variables: model the possible decisions
- $N$ variables $X_{1}, X_{2}, \ldots, X_{N}$ corresponding to the $N$ numbers
- Domains: model the possible choices for a decision
- For each variable, we can pick a value in $\boldsymbol{S}$ only
- Constraints: rule out incompatible choices
- ?


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- For each variable, we can pick a value in $\boldsymbol{S}$ only
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- $X_{1}+X_{2}+\ldots+X_{N}=K$ and all different values for $X_{1}, \ldots, X_{N}$


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- Domains: model the possible choices for a decision
- For each variable, we can pick a value in $\mathbf{S}$ only
- Constraints: rule out incompatible choices
- $X_{1}+X_{2}+\ldots+X_{N}=K$ and all different values for $X_{1}, \ldots, X_{N}$
- Parameters: the set $\mathbf{S}$ and numbers $\mathbf{N}$ and $\mathbf{K}$

